

# Data Exploration Through Descriptive Statistics and Graphics

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# Resources for statistical assistance

## Department of Statistics at UBC:

[www.stat.ubc.ca/how-can-you-get-help-your-data](http://www.stat.ubc.ca/how-can-you-get-help-your-data)

SOS Program - An hour of free consulting to UBC graduate students. Funded by the Provost and VP Research Office.

STAT 551 - Stat grad students taking this course offer free statistical advice. Fall semester every academic year.

Short Term Consulting Service - Advice from Stat grad students. Fee-for-service on small projects (less than 15 hours).

Hourly Projects - ASDa professional staff. Fee-for-service consulting.

# Outline

- ▶ Types of variables
- ▶ Plotting and summarizing a single variable:
  - ▶ **Categorical** variable
  - ▶ **Numeric** variable
- ▶ More than one variable:
  - ▶ Two or more categorical variables
  - ▶ One categorical and one numeric variable
  - ▶ Two numeric variables
- ▶ More than two variables when at least one is numeric

# Types of data

- ▶ Categorical data
  - ▶ **Nominal**: Label with no logical order (e.g. hair color)
  - ▶ **Ordinal**: Label, but the data can be sorted (e.g. happiness level)
- ▶ Numeric data
  - ▶ **Ratio**: Has a meaningful zero (e.g. height, income, distance)
  - ▶ **Interval**: Has an arbitrarily defined zero (e.g. temperature)
- ▶ Categorical and numeric data are treated very differently
- ▶ Usually distinctions between nominal/ordinal or interval/ratio will not make much difference

## Plotting in general

The purpose of graphics is not to be pretty or complicated but to convey information in a clear and unbiased way.

Graphics need not be fancy or complex to be effective. In fact the simplest graphic is usually the most effective.

Adding extra dazzle to a graphic can be distracting and make the graphic confusing and hard to interpret.

Every feature on a graphic should have a clear purpose. If it doesn't have a purpose, remove it.

Pie charts are an example of a graphic that contain added features that otherwise convey no information (3-D effects, for example).

## Plotting and summarizing one variable

With a single variable, the usual goal is to examine how the set of points are distributed and summarize some **features** of the data.

A feature could be the middle of the data, the dispersion of the data, the most common value or the frequency of an occurrence.

How we summarize and plot categorical variables is very different from how we summarize and plot numeric variables.

## Categorical data

For a nominal variable, each of the outcomes represents something qualitatively different. The outcomes have names or labels that cannot be compared, and have no relative order.

Ordinal data is quantitative data, because it can be ordered and allow logical comparisons between observations (e.g. small, medium, large). Note: Likert scales are ordinal variables, not numeric variables.

We cannot use arithmetic on categorical variables! “Small + medium = ...” does not make sense.

Categorical variables usually have many subjects with the same observed value for the variable. The **frequency** of occurrence is what interests us.

## Categorical data: Tabulating data

We tabulate categorical data by counting the occurrence of each unique value. Presenting the data as a percentage is usually more informative, but it does hide the sample size.

```
## Titanic:
```

```
## Number of passengers by Class
```

```
## Class
```

```
## 1st 2nd 3rd Crew Sum
```

```
## 325 285 706 885 2201
```

```
## Percentage of passengers by Class
```

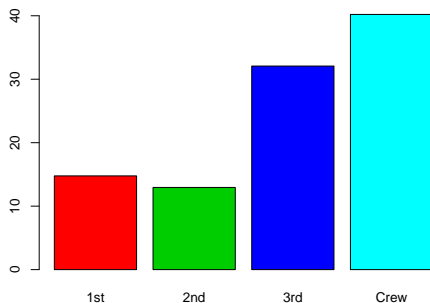
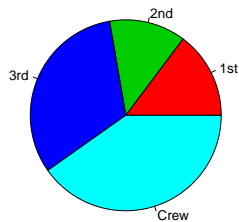
```
## Class
```

```
## 1st 2nd 3rd Crew Sum
```

```
## 14.8 12.9 32.1 40.2 100.0
```



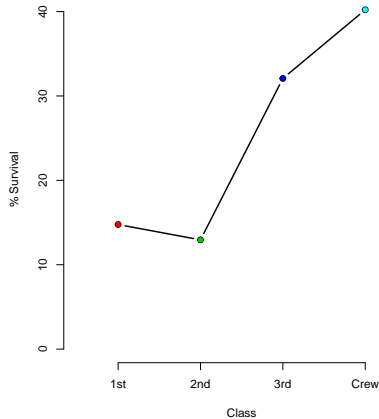
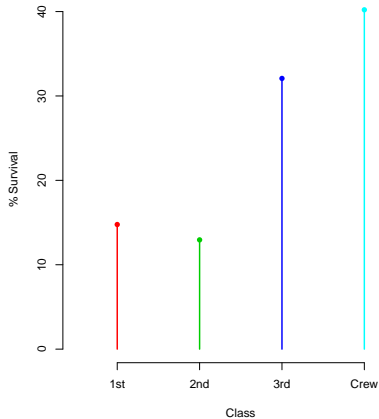
We can plot the data using either a pie chart or a bar chart



Which graphic do you find more informative?

The eye is good at judging linear measures and bad at judging relative areas.

## Dot chart or line chart



These use less ink but display the same information as a bar chart. The line chart allows several lines to be displayed simultaneously, which can provide better group comparisons than a bar chart or dot chart.

## Numeric data

A numeric variable gives real numbers that can be interpreted directly. Fifteen kilometers is 5 kilometers further than 10 kilometers. Fifteen degrees Celsius is 5 degrees warmer than 10 degrees Celsius.

They can be **discrete** or **continuous** (e.g. number of people in a room, number of correct answers on an exam, a person's height, time to complete a task).

Ratio data has a meaningful zero, which allows *relative* values to be interpreted. For example, 15 kilometers is 3 times as far as 5 kilometers.

However, ratios do not make sense for interval data: 15 degrees Celsius is not “three times as warm” as 5 degrees Celsius.

NOTE: Assigning numbers to an ordinal scale does not make it numeric. (i.e. Likert scales are not numeric.)

## Discoveries data set

The numbers of “great” inventions and scientific discoveries in each year from 1860 to 1959.

First eight years of the data set:

```
##  
## Year          1860 1861 1862 1863 1864 1865 1866 1867  
## Discoveries    5    3    0    2    0    3    2    3
```

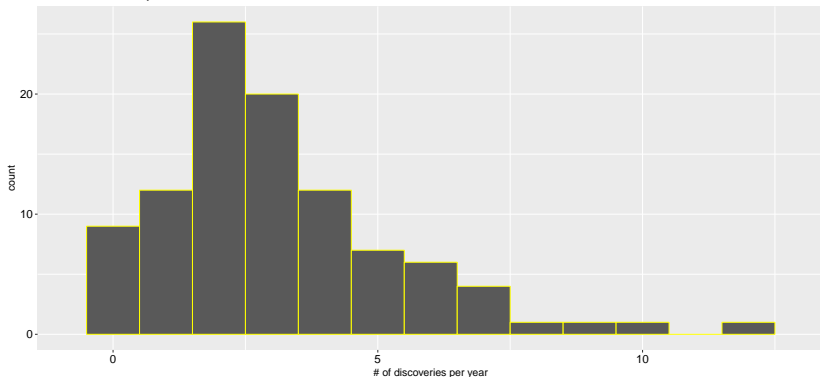
Tabulated results for number of discoveries per year (Count):

```
##  
## Discoveries 0  1  2  3  4  5  6  7  8  9 10 12  
## Count      9 12 26 20 12 7 6 4 1 1 1 1
```

# Plotting a numeric variable

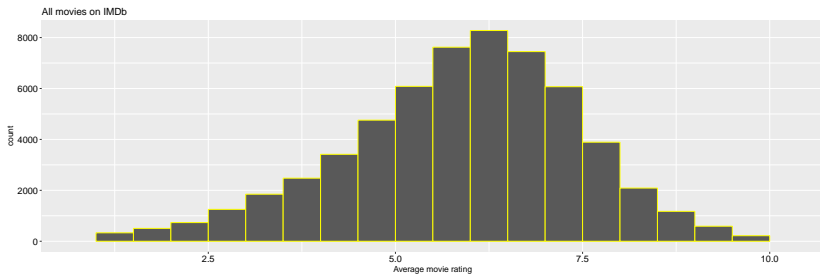
For discrete numeric variables with relatively few values, use a bar chart as we did for categorical variables.

# of 'great' inventions and scientific discoveries in each year from 1860 to 1959



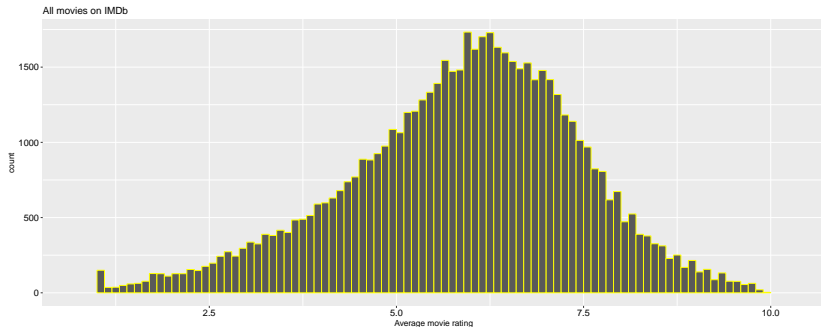
# Histograms

If we have continuous data, we can create small intervals and count the number of observations contained in each interval.



Most software will choose a bin width automatically, but you can change it if you like. Here I chose a bin width of 0.5.

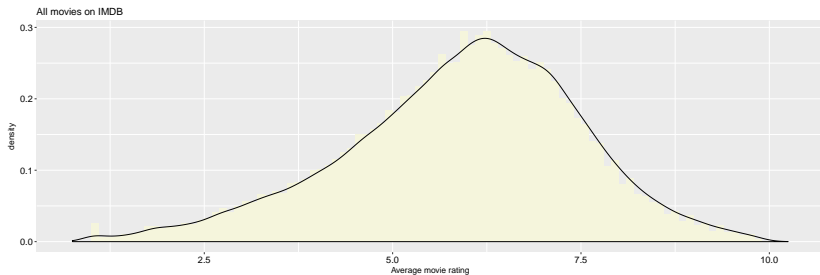
# The choice of bin width can be very important



With a large sample size ( $n=58,788$  for IMDb movies), we can choose a relatively small bin width. The graphic is not as “smooth”.

# Density plots instead of histograms

Put a smooth line through the tops of the bars in the histogram



Like a histogram, there are parameters that can be adjusted to control the smoothness of the plot. Most software provides reasonable defaults.



## Summarizing a numeric variable

Unlike a categorical variable, where all the information is captured in a table, we summarize numeric data into single values that describe a certain feature of the data.

We begin by finding the **central tendency** or “middle” of the data.

The most common measure is the **sample mean**, denoted by  $\bar{x}$ . It is computed by summing the data and then dividing by the sample size ( $\sum x_i/n$ ).

Another measure is the **median**. The median,  $\tilde{x}$ , is any value for which at least 50% of the data are  $\leq \tilde{x}$  and 50% of the data are  $\geq \tilde{x}$ .

## Example

## Data is  $X = \{ 5 \ 7 \ 8 \ 12 \ 18 \}$

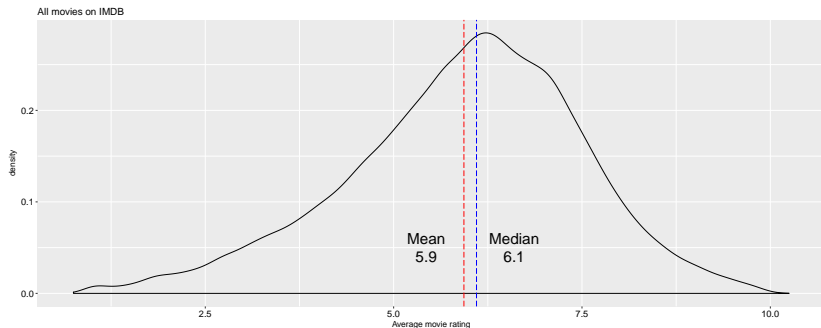
## Sum of  $X = 50$

## Mean of  $X = 10$

## Median of  $X = 8$

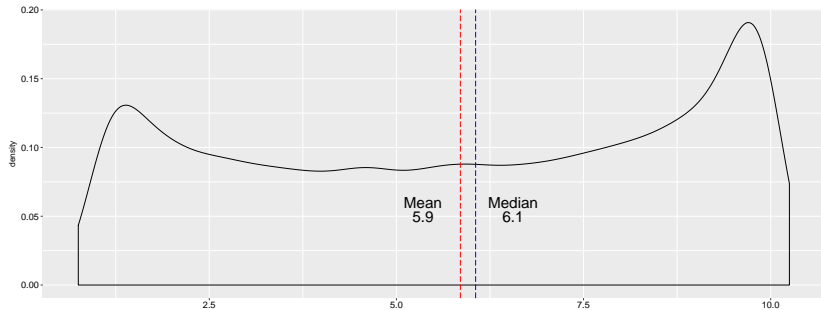
Note if the sample size is odd, the median is determined by a specific observation in the data. If the sample size is even, the median can be any value between the two middle values of the data. The common choice is the average of the two middle values.

# Add mean and median of the IMDB data with vertical lines



The mean is lower than the median here.

# The mode is not a good measure of central location



## Variation

After the central tendency, we usually describe the spread of the data.

The most common measure is the **standard deviation** (SD), denoted by  $s = \sqrt{\sum(x_i - \bar{x})^2 / (n - 1)}$ .

Other measures include the **inter-quartile range** (IQR) and the **median absolute deviation** (MAD).

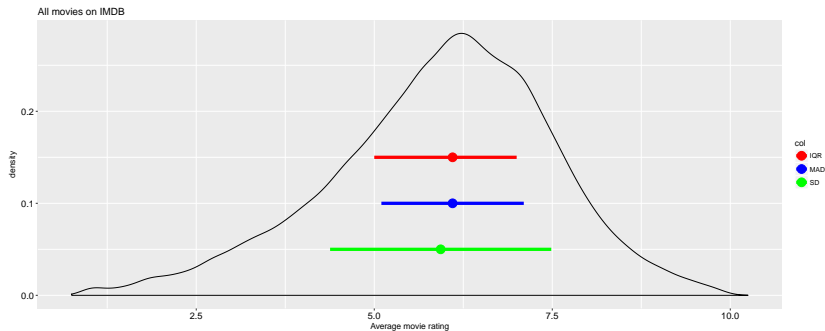
The **quartiles** are similar to the median, except they split the data into quarters instead of halves.

The median is the second quartile. The IQR is the difference between the 3rd and 1st quartile.

The MAD is calculated as  $\widetilde{|x_i - \tilde{x}|}$ .

# Summary statistics for the average rating in the IMDB data

##	N	Mean	Median	SD	IQR	MAD
##	58788	5.93	6.1	1.55	2	1



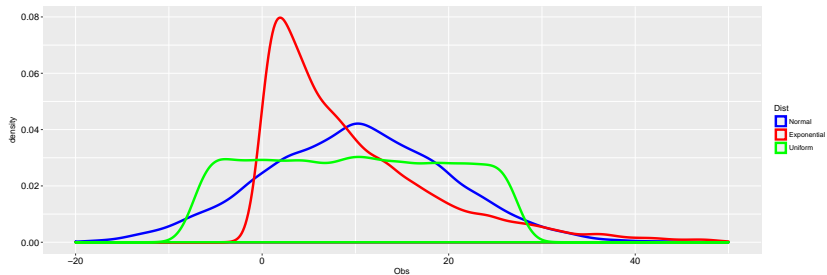
## Other numerical summaries

Other features used to describe numeric variables is the **skewness**, which measures the asymmetry in the data, and the **kurtosis**, which measures the “peakedness” of the data.

The mean, standard deviation, skewness and kurtosis are called **moments**. Together, they measure various attributes for the shape of a set of points. These are the first four moments. There are higher order moments, but they aren't typically used.

The median, quartiles and percentiles are collectively known as **quantiles**. Quantiles are used to more specifically describe how a set of points are distributed.

These distributions have very similar mean and sd



##	Dist	mean	sd
## 1	Normal	10.070928	9.960522
## 2	Exponential	9.954352	9.879440
## 3	Uniform	9.822214	10.010115



## We can distinguish the distributions by their skewness and kurtosis

```
##           Dist mean    sd  skew   kurt
## 1      Normal 10.07  9.96 0.0156  0.0118
## 2 Exponential  9.95  9.88 1.9287  5.5431
## 3      Uniform  9.82 10.01 0.0212 -1.1930
```

Skewness and kurtosis are not always easy to interpret.

Let's look at what the quantiles show:

```
##           10%  25%  50%  75%  90%
## Normal      -2.61  3.25 10.11 16.80 22.83
## Exponential  1.00  2.77  7.01 14.00 23.04
## Uniform     -4.01  1.12  9.80 18.46 23.81
```

## More than one variable

We are usually interested in looking at *relationships* in the data. How we examine the relationship might depend on the type of data we are considering and the roles they play.

- ▶ Are some variables considered responses while others are considered predictors?
- ▶ Do we want to see the form of the relationship between the variables, or just determine if some features are different for various subgroups?

Data should come in a **rectangular** format. In this format, each row is a sampled unit, and each column is a variable measured on that unit.

## More than one categorical variable

We cross-tabulate the occurrences.

```
## The fate of the passengers of the Titanic
```

```
##           Sex           Male           Female
##           Survived    No Yes      No Yes
## Class
## 1st           118    62           4 141
## 2nd           154    25           13  93
## 3rd           422    88          106  90
## Crew          670   192           3   20
```

Here we have the passengers split by Class, Sex and Survival, three nominal categorical variables. Sex and Survival have 2 levels (i.e. they are “binary”), while Class has 4 levels.

Percentages are more informative, but how should these be calculated?

**It depends on what you want to compare.**

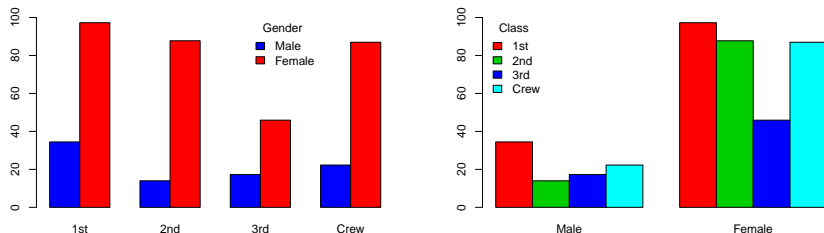
Let go back to the Titanic example. It makes sense that we want to draw conclusions about survival rates. Therefore we should compute our percentage of survival within Class and Sex.

```
## Survival percentage of Titanic passengers
```

```
##           Class
## Sex       1st  2nd  3rd  Crew
## Male    34.4 14.0 17.3 22.3
## Female  97.2 87.7 45.9 87.0
```

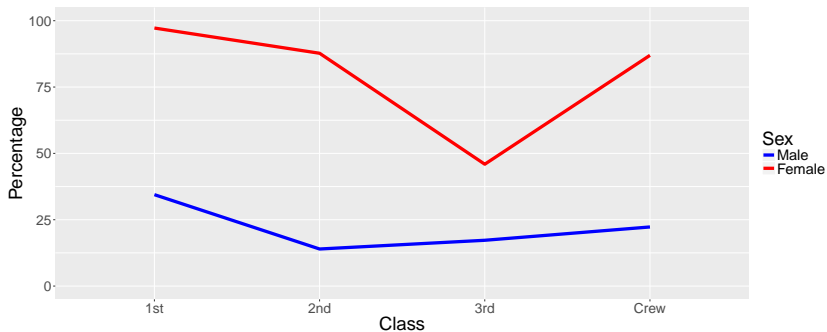
We can use a bar chart to display the data for more than one categorical variable, and distinguish the extra groups by colour

**Titanic: Percentage Passenger Survival**



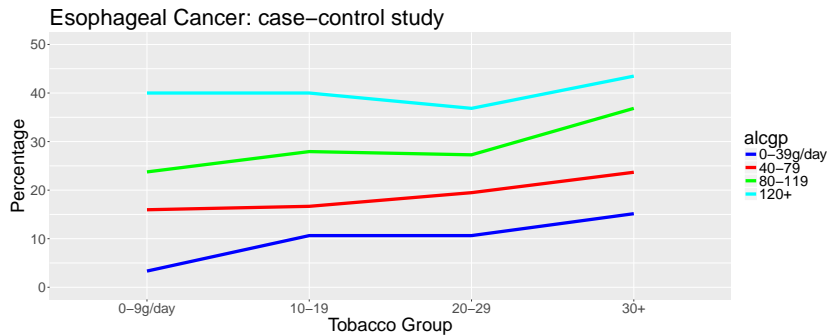
However, this could get very busy if we had more categories.

## We can use a line chart instead of a bar chart

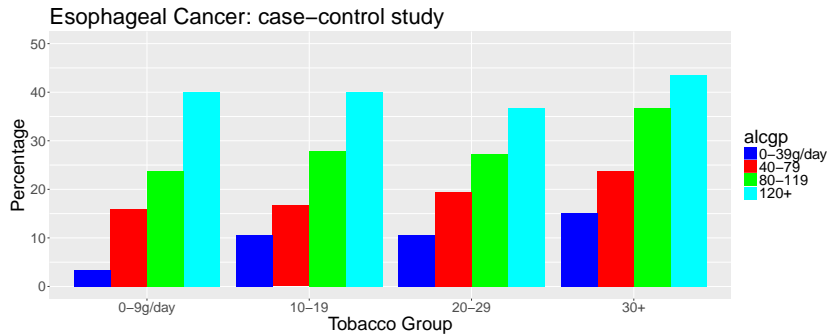


This type of plot can be handy if the number of categories becomes large.

# Controls and cases with esophageal cancer in 4 alcohol consumption groups by 4 tobacco consumption groups



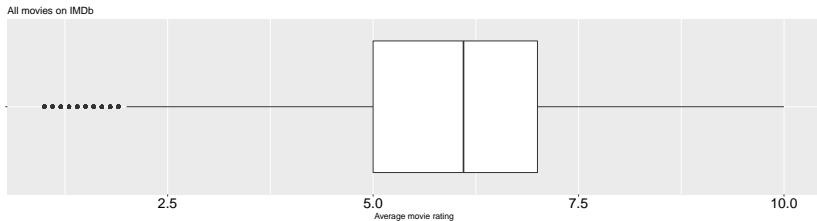
# Compare the previous line charts to a bar chart



Which do you prefer?



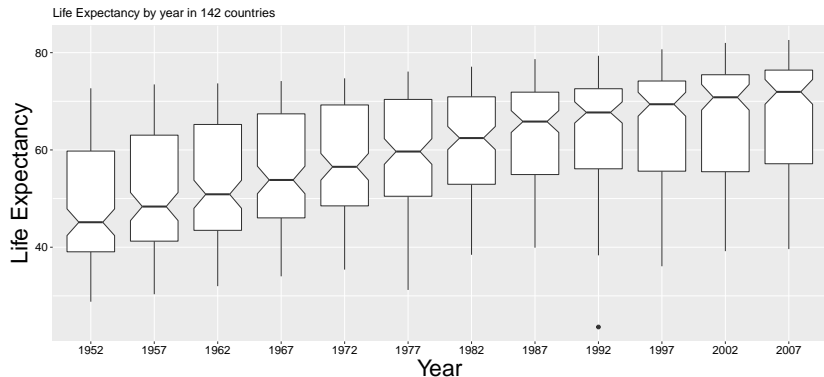
# One numeric variable and one categorical variable



You can plot a numeric variable using a **boxplot**. This is based on summary statistics of the data and is useful when comparing data between several groups.

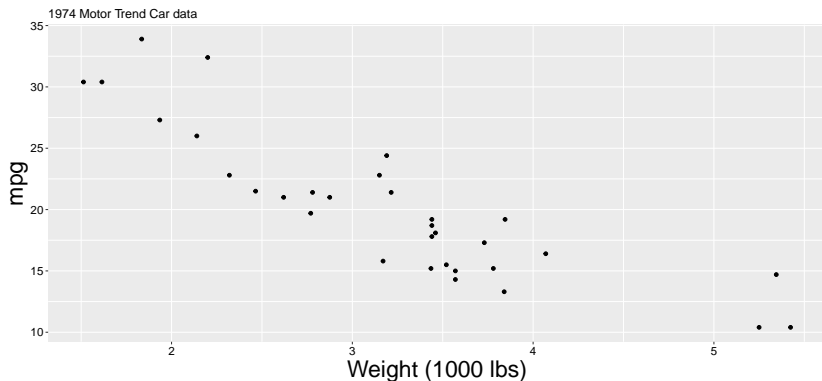
The central line is the median. The box covers the lower to upper quartile. The whiskers extend to an “acceptable” limit. Points outside these limits are possible outliers.

## Comparing a numeric variable across the levels of a categorical variable



We can quickly inspect the difference in location (median), dispersion (IQR) and skewness. The “notch” is a 95% confidence interval for the median.

# Scatterplots for two numeric variables



Select one variable for the y-axis and one for the x-axis. This defines a grid of possible values for  $(x, y)$  data pairs. Put a point on the grid for each data pair where the x-value and y-value cross.

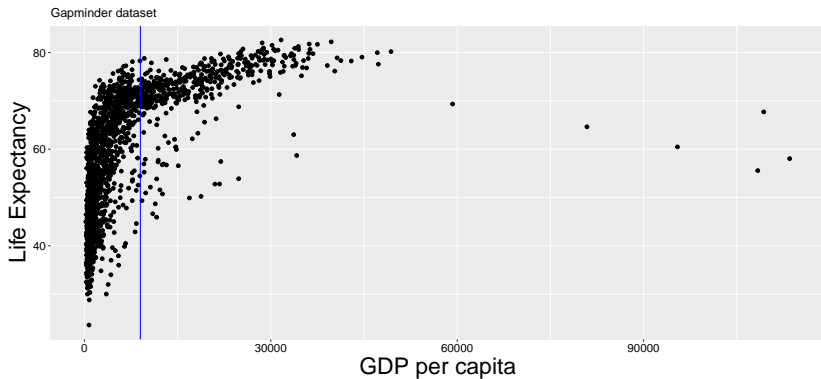
## We quantify the relationship between 2 continuous variables by the correlation

The usual **correlation** coefficient is the **Pearson product-moment correlation**  $r$ . It quantifies the linear relationship between 2 variables. ( $-1 \leq r \leq 1$ ) is a unitless quantity, where 0 means no relationship and  $\pm 1$  is a perfect linear relationship.

Other measures of correlation are Spearman's rank correlation ( $r_s$ ) and Kendall's  $\tau$ . Both measure how likely one variable will increase with another without requiring a linear relationship.

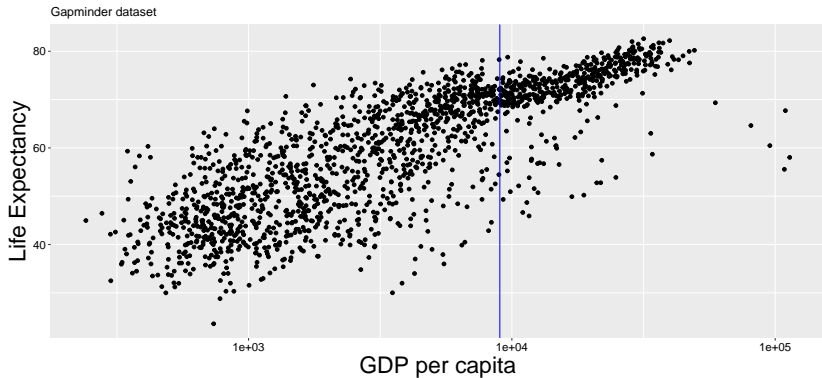
In the previous example, the correlation between mpg and weight by each measure is  $r = -0.87$ ,  $r_s = -0.89$  and  $\tau = -0.73$ .

# Gapminder data from Ted Talk



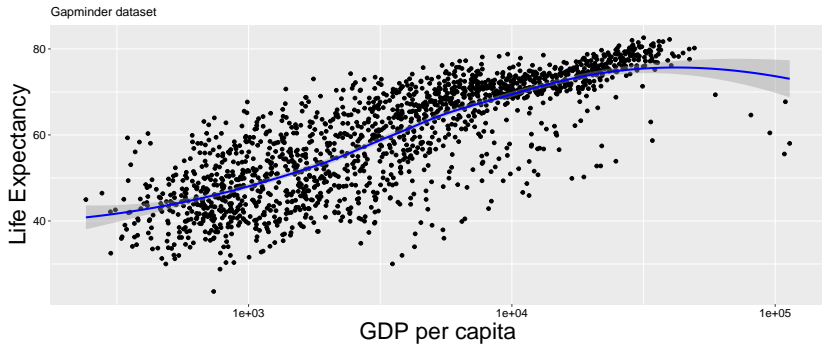
There is a definite relationship between life expectancy and GDP/capita but it is nonlinear. For this data  $r = 0.58$ ,  $r_s = 0.83$  and  $\tau = 0.64$

## Express the GDP/capita on a logarithmic scale



The relationship looks more linear and we have a better picture of the data at the lower values of GDP/capita. Now  $r = 0.81$ , while  $r_s = 0.83$  and  $\tau = 0.64$  do not change.

## Add a curve that approximates the relationship



We add a smooth curve estimated from the data. A linear fit seems reasonable, except at extremely large values of GDP/capita.

## More than 2 variables when at least one is numeric

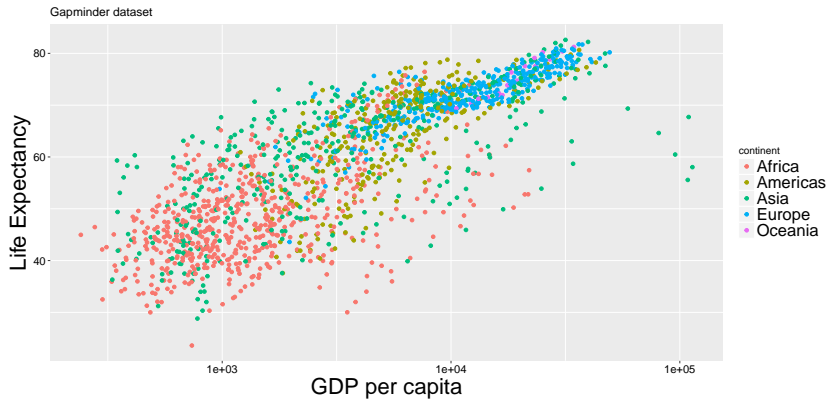
Each variable in a graphic uses one dimension of space, and most graphical devices are still only two-dimensional.

Previously with 3 categorical variables, we used colour to represent the third dimension. This is commonly done in graphics. Depending on the information we need to add, we can use colour, size or symbol to represent the additional data. Using all three, we can have up to 5 dimensions represented on the plot.

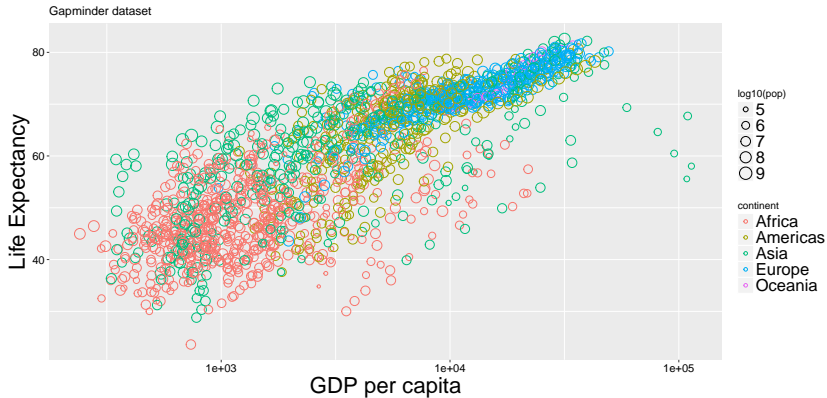
When designing such a plot, you need to make sure the graphic does not become too cluttered and hard to interpret. Different symbols are useful for a categorical variable with only a few categories. Size might be used to represent a positive numeric variable. Colour is the most versatile.



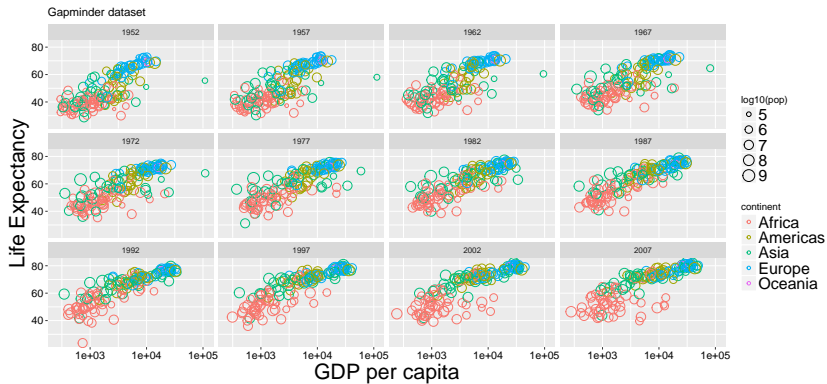
# Let's add continent information to the previous graphic



# Let's add population information to the previous graphic

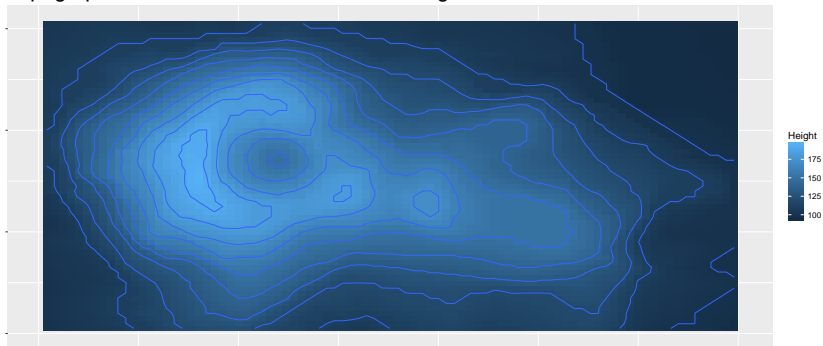


# One final detail is year



# Contour plots

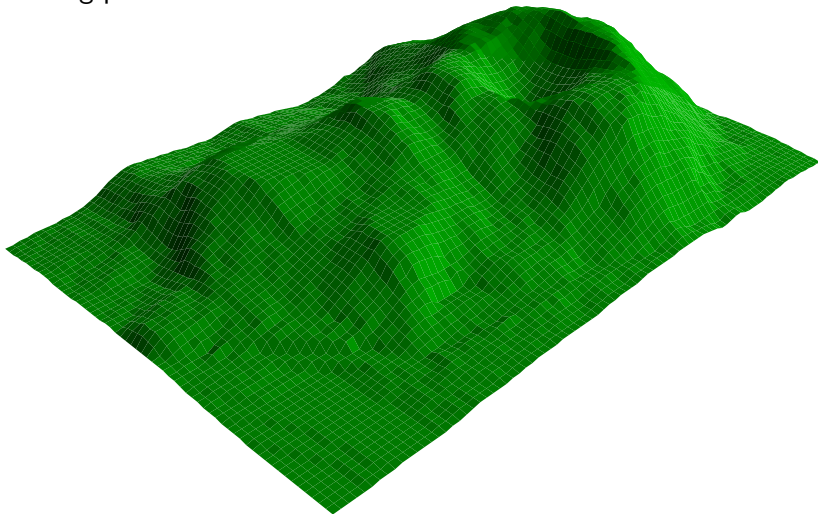
Topographic information on Auckland's Maunga Whau Volcano



If you have 2 dimensions that form a grid for a third numeric variable, you can use a contour plot.

## Perspective plots

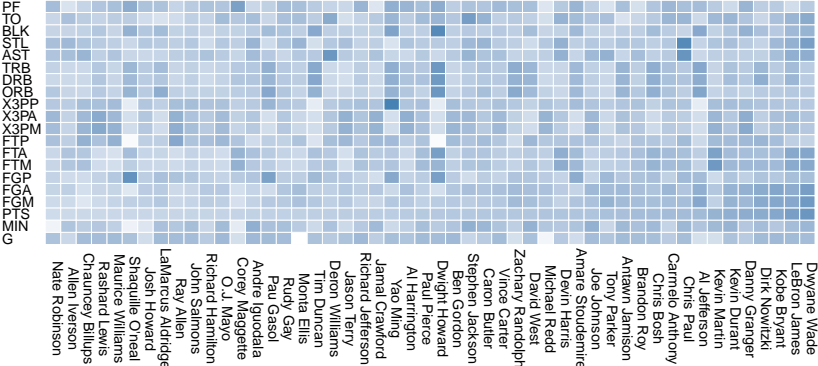
We can also use a perspective plot. The challenge is picking a good viewing point.



# Heatmaps

If you have 2 discrete dimensions, and you wish to display numerical information for each combination of the categorical variable, you can use a heatmap.

NBA top 50 scorers: 2008/2009



# Questions?

## Department of Statistics UBC:

[www.stat.ubc.ca/how-can-you-get-help-your-data](http://www.stat.ubc.ca/how-can-you-get-help-your-data)

STAT 551 - Stat grad students taking this course offer free statistical advice. Fall semester every academic year.

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